#### Intergenerational Mobility and Housing Wealth in the United States

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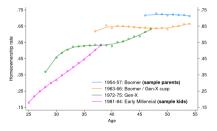
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Corresponding author: Ariel Binder, ariel.j.binder@census.gov. Any conclusions and opinions expressed herein reflect those of the authors and do not represent the views or official positions of the U.S. Census Bureau or the Internal Revenue Service. The Census Bureau has ensured appropriate access and use of confidential data and has reviewed these results for disclosure avoidance protection (Project 7529092: CBDRB-FY24-CES014-005 and CBDRB-FY24-CES023-001).

#### Housing, wealth and intergenerational inequality in the U.S.

- Housing is a primary asset for all but top wealth holders.
  - Saez and Zucman (2016):  $\sim$  40% for households in bottom 90%.
  - 2022 SIPP: 29% of wealth held by 99%. Median renter wealth: \$9K. Median homeowner wealth: \$398K, 60% of which is housing.
  - 2022 SCF: 32%. Retirement wealth correlated  $\sim$  0.6 with housing wealth.
- Considered stepping stone to building generational wealth, but has become less attainable.



Source: public-use 2000 Long Form and 2005-2022 American Community Survey files. Sample restricted to those born in the U.S.

#### Housing, wealth and inequality in the U.S.

- Homeownership inequality: cause and consequence of persistent wealth and income inequality.
- Much research on intergenerational mobility (IGM) of income; less is known about IGM of wealth.
  - Wealth is potentially a better proxy for total resources.
  - Housing does not generally return income.
- Huge wealth gap between Black and White households.
  - Legacy of financial exclusion and segregation.
  - Persistence in gap (Derenoncourt et al. 2024) suggests differential IGM.

#### This paper

Linked data on housing assets, survey and tax records for 3.4 million U.S. families.

- IGM of housing assets.
  - Rank-Rank relationships.
  - Racial disparities (focus on White versus Black today).
- IG relationships between income and wealth.
  - Income IGM an attenuated measure of total resource IGM.
  - Static IG capital accumulation model.
  - Simple decomposition of IG wealth transmission.
  - Implications for racial disparities.
- Local variation.
  - Sample size allows us to estimate county-race-level mobility statistics.
  - Analyzing these in ongoing work.



#### Key findings

- 1. Housing wealth exhibits greater IG persistence than income.
- 2. Large gaps in absolute and relative mobility between Black and White families.
  - Contrast to income gaps.
  - Extensive margin of home ownership important.
- 3. Parental capital wealth shapes child resources
  - through its effects on child labor income
  - but at least much through "direct" resource transmission.
  - Direct channels crucial for racial gaps.
- 4. Housing IGM varies substantially across U.S. counties.
  - Great Recession shock.
  - Housing supply constraints.
  - Racial segregation.



#### Contribution to literature

- IGM with focus on income, wealth, and race.
  - Income IGM: Bhattacharya and Mazumder (2011), Davis and Mazumder (2018), Chetty et al. (2020), Collins and Wanamaker (2022), Derenoncourt (2022).
  - Wealth IGM: Pfeffer and Killewald (2018, 2019), Killewald and Bryan (2018).
  - Income and the racial wealth gap: Barsky et al. (2002), Derenoncourt et al. (2022), Sabelhaus and Thompson (2022).
  - Income versus transfers: Charles and Hurst (2003), Feiveson and Sabelhaus (2018), Black et al. (2020, 2022), Gilraine et al. (2023).
- Administrative housing data to study IGM or racial disparities.
  - Housing IGM: Daysal et al. (2022, 2023), Benetton et al. (2022), Wold et al. (2023)
  - Cross-sectional racial disparities: Avenancio-Leon and Howard (2024), Kermani and Wong (2024), Box-Couillard and Christensen (2024).
- Capitalizing income flows to estimate cross-sectional wealth distribution.
  - Piketty and Zucman (2014), Saez and Zucman (2016), Smith et al. (2023).
  - We are the first to study IGM in this context.



# Data and Empirical Strategy

#### Data overview

- Sample of children (g) and their parents (g-1).
  - 2000 Census Long Form (LF): all householders' children aged 14-16.
  - Opportunity Insights Databank (DB): all dependents aged 14-16 claimed on a 1994 or 1998 tax return
    - whose claimer was also a LF householder.
- Administrative housing records.
  - 2019-2021 property assessment, deed, and valuation files from Black Knight, Inc (BK).
  - Census linkage branch assigned Protected Identification Keys (PIKs) to these records.
  - Ownership determined by (PIK) of owner on assessment file or PIK of buyer on deed file.
  - Valuation imputed from assessed / sold values where missing. Petails
- Contemporary income information.
  - 2018, 2019, 2021 tax records available in the DB.

#### Final sample characteristics

- 3.4 million parent-child pairs.
- Race-ethnicity, geography, birth year, homeownership and assets, family income, capitalized wealth.
- Incomes averaged across 3 years of data.
- Children born in 1978-86, aged 34-42 in 2020.
- Parent mean (SD) age in 2000: 46.3 (7.2).
- Sample requires:
  - Valid PIK for parent and child,
  - Parent being in filing population at least once,
  - Parent being a householder in 2000.

#### Housing measurement details / limitations

- Child wealth concept comes from Black Knight.
  - Business ownership cannot be PIK'd without info on business structure.
  - Focus on "personal" wealth holdings.
  - Property versus housing.
  - No debt data.
- Parent wealth concept comes from 2000 LF.
  - Tenure question gives us ownership info. Follow-up question about home value.
  - 25 different bins of home value.
  - Cannot learn about remote / multiple ownership.
  - Assume household reference person is homeowner.

#### Housing measurement details / limitations

- Assigning ranks.
  - Let x = ownership rate.
  - Assign non-owners rank of (1-x)/2.
  - Owners ranked 1 x + 1/N up to 1 by asset values.
- Imperfect assignment of PIKs to property records.
  - Assignment algorithm works best when we have SSN and/or {DOB, full name, location}.
  - Only observe {full name, location}.
  - Merge of ACS housing info onto our sample reveals slight under-count of owners:

| 2021  |     | BK owner |       | 2020  |     | BK owner |       |
|-------|-----|----------|-------|-------|-----|----------|-------|
|       |     | No       | Yes   |       |     | No       | Yes   |
| ACS   | No  | 0.353    | 0.058 | ACS   | No  | 0.330    | 0.069 |
| owner | Yes | 0.112    | 0.477 | owner | Yes | 0.113    | 0.488 |

Source: American Community Survey linked to Black Knight property records.

#### Weighting estimator: simple example

- Ignore intensive margin for now.
- Start with ownership rate estimate from survey data.
  - Children sampled by 2018-2021 ACS.
  - Some individuals may not own their ACS address but remotely own property.
  - Estimate this population in 2018 SIPP, get  $a_{SIPP} = \frac{x_{SIPP} + r_{SIPP}}{x_{SIPP}}$ .
  - Construct  $x_{ACS^*} = x_{ACS} \cdot a_{SIPP}$ .
- "Final" weight,  $fw_i$ , =
  - $bw_i \cdot \frac{1 x_{ACS}*}{1 x_{BK}}$  if kid *i* is not a BK owner
  - $bw_i \cdot \frac{x_{ACS^*}}{x_{BK}}$  if kid *i* is a BK owner
  - where  $bw_i$  is a base weight.

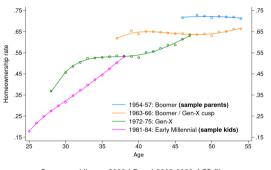
#### Weighting estimator: adding detail

- Wish to estimate ownership cdf  $H_{g-1}(x) = H(x|g-1)$ .
- Iterate the reweighting procedure within 550 bins defined by  $\{$  White, Black, Hispanic, Asian, Other  $\} \cdot \{$  nonowner, 10 deciles of parental housing wealth  $\} \cdot \{$  10 deciles of parental income  $\}$ .
- To estimate valuation cdf F(v|g-1,x), implement intensive margin adjustment as well.
  - Compare ACS owners' home values across owners who differ in BK ownership status.
  - If most "unlinked" owners are relatively poor, up-weight observed poorer BK owners and down-weight observed richer BK owners.

▶ Intensive margin details

#### Weighting estimator: life-cycle adjustment

Figure: Age-Ownership Profile for Selected Cohorts

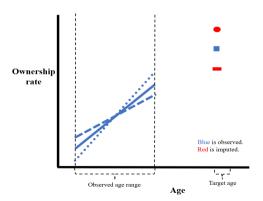


- Source: public-use 2000 LF and 2005-2022 ACS files. Sample restricted to those born in the U.S.
- Major re-ranking when purchase first house that likely scales with parental wealth.
- Adjust the extensive margin weights to "target" age 45-49 ownership rates in ACS.



#### Weighting estimator: life-cycle adjustment

- ullet Challenge: individuals are too old to observe target ownership rate by g-1 status.
- Solution: extrapolate based on differential observed age-ownership profiles.
- If  $x_a^{1978} x_a^{1986} > \overline{x}^{1978} \overline{x}^{1986}$ , add a larger-than-average constant to a's observed rate  $x_a$ .



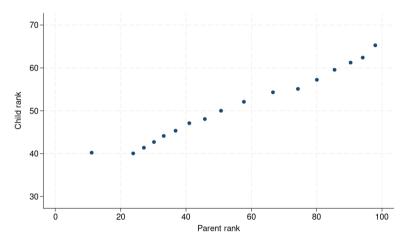
#### Empirical design: Rank-rank intergenerational mobility

$$Y_{g} = \alpha + \beta Y_{g-1} + u_{g} \tag{1}$$

- Absolute Mobility ( $\alpha$ ): average rank of children with worst-off parents.
- Relative Mobility  $(\beta)$ : gain in child rank associated with a one-rank gain in parent rank.
- Consider various measures of Y including housing assets, income, and wealth.
- Ranks always defined at the full population level.

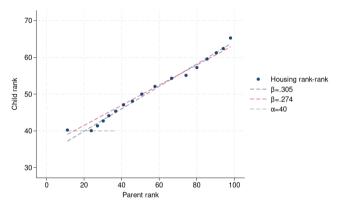
# Intergenerational Mobility of Housing Wealth in the U.S.

## Extensive margin, absolute Mobility ( $\alpha$ ), and relative mobility ( $\beta$ )



Source: IRS federal income tax records linked to 2000 LF and BK property records.

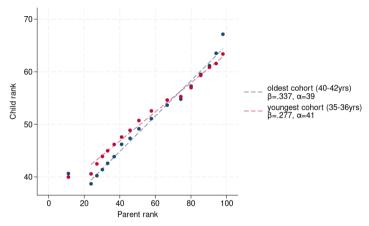
### Extensive margin, absolute mobility $(\alpha)$ , and relative mobility $(\beta)$



Source: IRS federal income tax records linked to 2000 LF and BK property records.

- Add a "parent renter" fixed effect to equation (1).
- "Worst-off" parents are those that own the cheapest houses.

#### Life-Cycle accumulation of housing assets

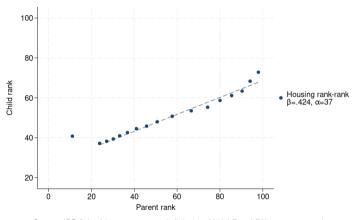


Source: IRS federal income tax records linked to 2000 LF and BK property records.

- Suggests attenuation bias. → Table
- But we don't find this relationship for income.



#### Rank-Rank estimates of housing IGM

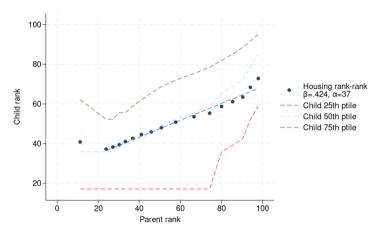


Source: IRS federal income tax records linked to 2000 LF and BK property records.

- Income comparisons:
  - Chetty et al. (2020):  $\beta$ =0.35,  $\alpha$ =32.5.
  - Our data:  $\beta$ =0.358,  $\alpha$ = 32.2. Figure

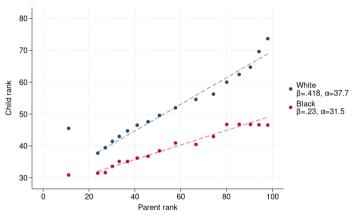


#### Rank-Rank estimates of housing IGM



- Compression of conditional distribution at top.
- Don't see this as much for income.

#### Racial gaps in IGM of housing

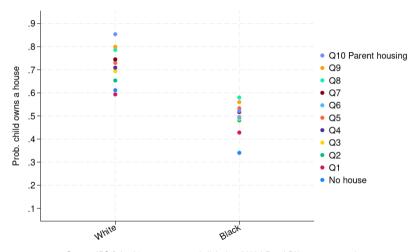


Source: IRS federal income tax records linked to 2000 LF and BK property records.

- Income comparisons:
  - Chetty et al. (2020): White  $\beta$ =0.32,  $\alpha$ =36.8; Black  $\beta$ =0.28,  $\alpha$ =25.4.
  - Our data: White  $\beta$ =0.322,  $\alpha$ =36; Black  $\beta$ =0.274,  $\alpha$ =22. Figure

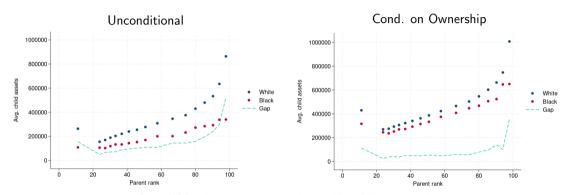


### Racial gaps in the probability of child home ownership



Source: IRS federal income tax records linked to 2000 LF and BK property records.

#### Average child housing assets by parent rank and race

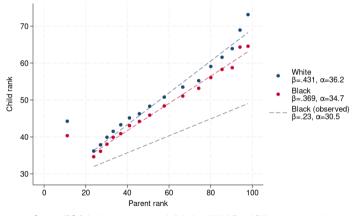


Source: IRS federal income tax records linked to 2000 LF and BK property records.



#### How important is extensive margin for observed differences in IGM?

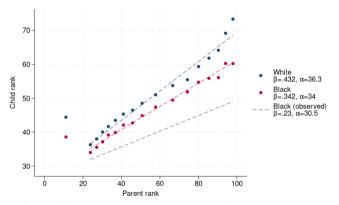
- Equalize Black and White child ownership rates | parent housing rank.
- CF1: assign new Black home owners average home value of observed Black homeowners.



Source: IRS federal income tax records linked to 2000 LF and BK property records.

#### How important is extensive margin for observed differences in IGM?

• CF2: capitalize rents paid by Black renters.

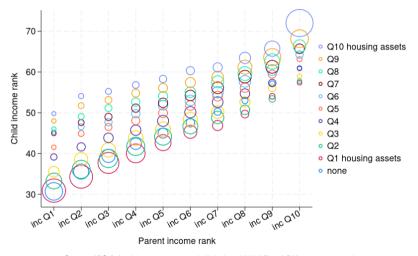


Source: IRS federal income tax records linked to 2000 LF and BK property records.

• Reduces conditional gap  $\approx$ 66% through most of the distribution,  $\approx$ 55% in top 10%.

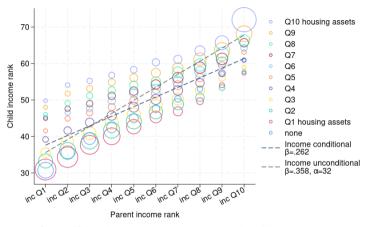
# Intergenerational Relationships between Income and Wealth

#### Joint relationship of parent housing and parent income on child income



Source: IRS federal income tax records linked to 2000 LF and BK property records.

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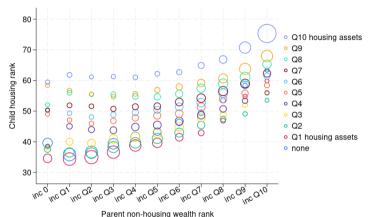


Source: IRS federal income tax records linked to 2000 LF and BK property records.

• Income-Income unconditional  $\beta$ =.36; conditional on housing  $\beta$ =.26. • Table



#### Joint relationship of parent housing and parent income on child housing



Parent non-nousing wealth rank

Source: IRS federal income tax records linked to 2000 LF and BK property records.

• Conditional Coefficients, Income: 0.181\*\*\* (0.001); Housing: 0.290\*\*\* (0.001) ▶ Table

#### Simple model of child asset accumulation

Take generation g's lifetime budget constraint as:

$$c_g + b_g = s_g Y_g (1+r) + (1-s_g) Y_g + b_{g-1}$$

- $c_g$ : Lifetime consumption
- $b_g$ : Wealth bequest to next generation
- $Y_g$ : Lifetime earnings, saved at rate  $s_g$
- r: rate of return on savings
- $b_{g-1}$ : Inherited wealth from previous generation

#### Parent influences on child resources

1) Children imperfectly inherit labor market productivity from parents.

$$Y_g = f(W_{g-1}) + u_g = \rho_y W_{g-1} + u_g$$

Children use their earnings to accumulate wealth, but may obtain additional wealth, from:

2) A direct transfer from parents:

$$b_{g-1} = f(W_{g-1}) = \rho_b W_{g-1}$$

3) Parental-wealth-induced saving behavior, i.e.

$$s_g = f(W_{g-1}) + \nu_g = \rho_s W_{g-1} + \nu_g$$

#### Simultaneous equation model

Child earnings are a function of parent wealth:

$$Y_g = \rho_y W_{g-1} + u_g. \tag{2}$$

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$$Y_g = \rho_y W_{g-1} + u_g. \tag{2}$$

Child wealth is a function of child earnings and parent wealth:

$$W_g = f(Y_g, W_{g-1}) = (1+r)s_g Y_g + b_{g-1}$$
$$= (1+r)(\rho_s W_{g-1} + \nu_g)Y_g + \rho_b W_{g-1}$$
$$= (1+r)\bar{s}Y_g + \rho_b W_{g-1} + (1+r)\rho_s (Y_g \times W_{g-1})$$

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=  $(1+r)(\rho_s W_{g-1} + \nu_g)Y_g + \rho_b W_{g-1}$   
=  $(1+r)\bar{s}Y_g + \rho_b W_{g-1} + (1+r)\rho_s (Y_g \times W_{g-1})$ 

Which gives the following regression:

$$Y_g = \beta W_{g-1} + u_g$$

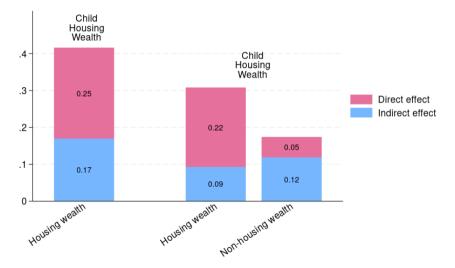
$$W_g = \gamma_y Y_g + \rho_b W_{g-1} + \gamma_s (Y_g \times W_{g-1}) + \epsilon_g.$$
(3)

## Simultaneous equation model: direct and indirect effects

$$Y_g = \rho_y W_{g-1} + u_g$$
 
$$W_g = \gamma_y Y_g + \rho_b W_{g-1} + \gamma_s (Y_g \times W_{g-1}) + \epsilon_g$$

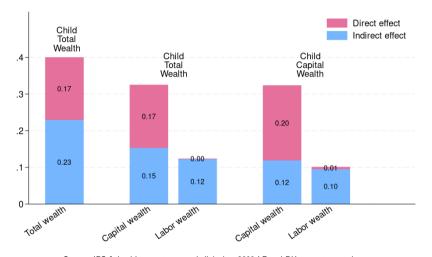
- "Direct Effect": Impact of parent wealth on child wealth, independent of child income ( $\rho_b$ ).
- "Indirect Effect": Impact of parent wealth on child wealth through child earnings ( $\rho_y * \gamma_y$ ).
  - Parent wealth increases child earnings  $(\rho_y)$ .
  - Child earnings purchase wealth  $(\gamma_y)$ .
- These effects decompose the relative mobility coefficient  $\beta$  from equation (1):  $W_g = \alpha + \beta W_{g-1} + e_g$ .

# Direct and indirect effects of parent resources on child housing



Source: IRS federal income tax records linked to 2000 LF and BK property records.

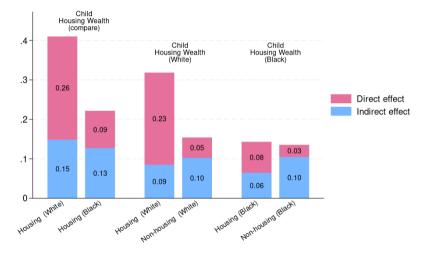
## Direct and indirect effects of parent resources on child total wealth



Source: IRS federal income tax records linked to 2000 LF and BK property records.

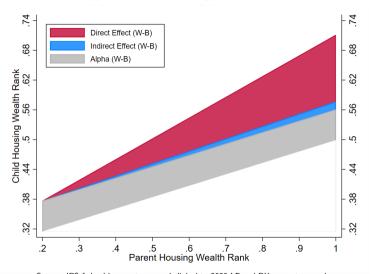


## Direct and indirect effects of parent resources on child housing, by race



Source: IRS federal income tax records linked to 2000 LF and BK property records.

## Decomposing racial IGM gaps in housing assets



Source: IRS federal income tax records linked to 2000 LF and BK property records.



# **Exploring Cross-County Variation**

## Constructing a cross-area dataset

- Estimate IGM equations (1), (2), and (3) separately by county.
- Require at least 30 unweighted observations. Weight by  $\sqrt{N_c}$ .
- Yields cross-county distributions of  $\rho$ ,  $\beta$ ,  $\rho_y$ ,  $\gamma_y$ ,  $\rho_b$ .
- Merge on county-level exposures:
  - Great Recession unemployment shock: p.p. change in UR, Jan 2007-Dec 2009.
  - Housing unit supply elasticity: aggregated to counties from tract-level estimates in Baum-Snow and Han (2024).
  - Racial segregation: county-level dissimilarity index across tracts (Binder et al. 2024).

## Cross-Area analyses

$$\beta_c = \phi + \theta_\beta E_c + \xi_c. \tag{4}$$

- $\theta_{\beta}$ : association between 1-unit change in given exposure and change in relative (im)mobility.
- $\theta_{\rho_b}$ : change in direct effect.  $\theta_{\beta} \theta_{\rho_b} = \theta_{\iota}$ : change in indirect effect.
- Indirect effect composed of "income levels"  $(\rho_y)$  and "income returns"  $(\gamma_y)$  channels.
  - Exposure may influence each channel.
  - With a technical assumption, a simple decomposition results:

$$\theta_{\beta} = \theta_{\rho_b} + \frac{\theta_{\iota} + \theta_{\rho_y} \overline{\gamma_y} - \theta_{\gamma_y} \overline{\rho_y}}{2} + \frac{\theta_{\iota} + \theta_{\gamma_y} \overline{\rho_y} - \theta_{\rho_y} \overline{\gamma_y}}{2}.$$
 Details (5)

- Estimate (4) and (5) separately for Whites and Blacks. Compute effect of exposure on
  - Racial mobility gap at bottom and at top
  - And decomposition of top gap.

### Full-Population results

Table: Associations between County-Level Exposures and Housing Wealth Mobility

| Exposure  | eta and its decomposition |                    |                    |                    |                    |
|---|---------------------------|--------------------|--------------------|--------------------|--------------------|
|   |                           | Total              | Direct effect      | Income returns     | Income levels      |
| GR unemployment shock (p.p. increase / 100)         | 697***<br>(.044)          | 0.945***<br>(.093) | 0.181***<br>(.069) | .259***<br>(.028)  | .505***<br>(.032)  |
| Exposure mean, SD, N: .046, .022, 3100              |                           |                    |                    |                    |                    |
| Housing supply elasticity (dlog units / dlog price) | 036*<br>(.021)            | 305***<br>(.031)   | 142***<br>(.022)   | 071***<br>(.013)   | 092**<br>(.025)    |
| Exposure mean, SD, N: .310, .123, 800               |                           |                    |                    |                    |                    |
| Racial segregation (W / nW dissimilarity index)     | 109***<br>(.006)          | 0.294***<br>(.015) | 0.115***<br>(.010) | 0.033***<br>(.005) | 0.146***<br>(.009) |
| Exposure mean, SD, N: .426, .173, 3100              |                           |                    |                    |                    |                    |

Mobility data source: IRS federal income tax returns linked to 2000 Census Long Form and Black Knight property records.

Great Recession shock data source: BLS Local Area Unemployment Statistics

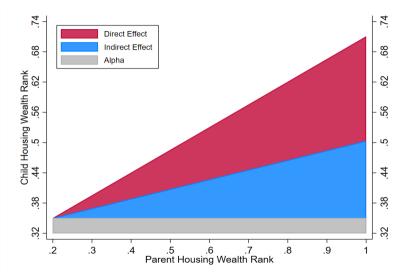
Housing supply data source: Baum-Snow and Han (2024)

Racial segregation data source: Binder et al. (2024), who use IRS federal income tax returns linked to Census race and ethnicity files.

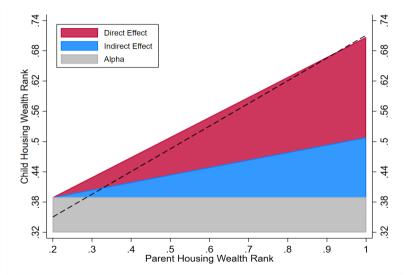




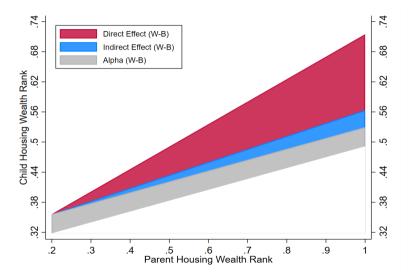
# Full population: High GR exposure



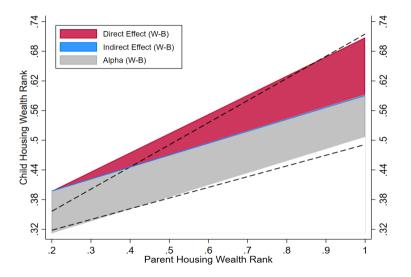
## Full population: Low GR exposure



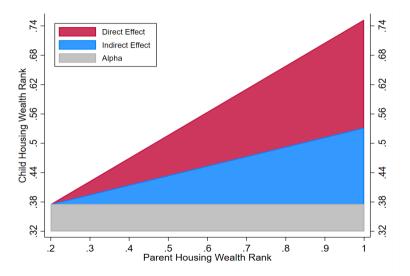
# Racial disparity: High GR exposure



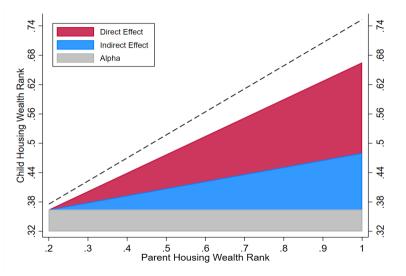
## Racial disparity: Low GR exposure



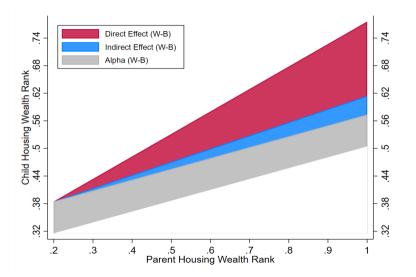
## Full population: Inelastic housing supply



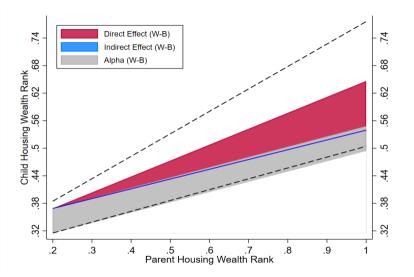
## Full population: Elastic housing supply



# Racial disparity: Inelastic housing supply



## Racial disparity: Elastic housing supply



# Conclusion / Next Steps

- Housing and other capital wealth plays an important role, independent of income flows, in generating IG persistence in economic resources among U.S families.
- Implications for racial disparities, spatial variation, and housing and macro stabilization policies.
- Robustness analyses:
  - Attempt to make some statements about IGE as well as rank-rank mobility.
  - LCA weights: Alternative method of constructing target ownership rates  $t_{ACS^*}^{g-1}$ ; implement an intensive margin adjustment.
  - Cross-area analyses: Empirical Bayes procedure to shrink the cross-area mobility distribution. CZ-level measure of segregation.
- Avenues for further work:
  - Relax the  $(\alpha, \beta)$  framework to allow non-linearity; interact our indirect / direct approach with quantile decomposition methods.
  - Further analyses on role of extensive margin.
  - Great Recession diff-in-diff.
  - Push the housing supply narrative further; augment the model to include location, housing supply, and human capital investment.

# Appendix

#### Imputing property valuations

- Valuation file contains most recent automated valuation model (AVM) estimate of market value. Virtually always
  corresponds to vintage year.
- AVM estimate is based on recent transaction of similar properties, weighted by recency of sale and similarity to given property.
- Small but non-negligible share of properties in assessment and deed files have missing valuations.
- Assessment (deed) file contains virtually always nonmissing information on last assessed (sold) value, and date of assessment (sale).
- Imputation procedure. For each county c:
  - Within each county c:
  - Estimate  $\ln(v_{pcy}) = \lambda_{0c} + \lambda_{1c} \ln(a_{pcy}) + \lambda_{2c} t a_{pcy} + \lambda_{3c}' Y + \epsilon_{pcy}$
  - Estimate  $\ln(v_{pcy}) = \nu_{0c} + \nu_{1c}\ln(s_{pcy}) + \nu_{2c}ts_{pcy} + \nu_{3c}'Y + e_{pcy}$
  - Where p is property, y is vintage year, a(s) is last assessed (sold) value,  $ta_{pcy}(ts_{pcy})$  is y minus the year of the last assessment (sale), as recorded in vintage y, and Y is a set of vintage year fixed effects.
  - Impute missing valuations as the assessment prediction, sale prediction, or a simple average of the two, depending on whether *a*, *s*, or both are non-missing.

▶ Back



### Intensive margin weighting adjustment

- Consider ACS owned home value distribution function A(v).
- Consider two conditional distribution functions,  $A_1(v) = A(v|ACS \text{ owner is a BK owner})$  and  $A_0(v) = A(v|ACS \text{ owner is not a BK owner})$ .
  - Consider a sequence of Q+1 uniformly-spaced quantiles  $q_0,q_1,\ldots,q_Q$ . That is,  $A_1(q_n)-A_1(q_{n-1})=1/Q$ .
  - It follows that  $A(q_n) A(q_{n-1}) = \frac{N_1/Q + N_0(A_0(q_n) A_0(q_{n-1}))}{N_1 + N_0}$  where  $N_1$  and  $N_0$  are respective sample sizes.
- Assumption: Consider a sequence of Q+1 quantiles  $p_0, p_1, \ldots, p_Q$  of the observed BK valuation distribution.  $\frac{N_1/Q+N_0(A_0(q_n)-A_0(q_{n-1}))}{N_1+N_0}$  is an unbiased estimate of  $F(p_n)-F(p_{n-1})$ .
- This assumption dictates setting  $fw_i = bw_i \cdot \frac{x_{ACS^*}}{x_{BK}} \cdot \frac{N_1/Q + N_0(A_0(q_n) A_0(q_{n-1}))}{N_1 + N_0}$  if kid i is a BK owner with housing assets in the [n-1,n) quantile range.
- As for the extensive margin, perform the intensive margin adjustment within each of 550 g-1 subgroups.
- Set  $Q = \lfloor N_{g-1}/15 \rfloor$  where  $N_{g-1}$  is the number of BK owners with characteristics g-1.
- Set intensive margin weight to 1 if  $N_{g-1} < 30$ .

▶ Back

## Life-Cycle weighting adjustment

- Let  $t_{ACS^*}$  = target ownership rate.
- Define  $\Delta_{ACS*} = t_{ACS*} x_{ACS*}$  and  $\delta^c_{ACS*} = x^{oldest}_{ACS*} x^{youngest}_{ACS*}$ .
- By construction,  $t_{ACS^*} = x_{ACS^*} + \Delta_{ACS^*} \cdot \frac{\delta_{ACS^*}^c}{\delta^c}$ .
- Assumption: for given subgroup g-1,  $t_{ACS^*}^{g-1} = x_{ACS^*}^{g-1} + \Delta_{ACS^*} \cdot \frac{\delta_{ACS^*}^{c,g-1}}{\delta_{CS^*}^{c,g-1}}$ .
- I.e., a subgroup whose ownership rate grew faster than the sample average is assigned a higher than average  $\Delta$  to add to its base ownership rate.
- In implementation, allow  $t_{ACS^*}$ ,  $\Delta_{ACS^*}$ , and  $\delta^c_{ACS^*}$  to vary by race.
- This yields the following life-cycle-adjusted weights:
  - $lcaw_{i(g-1)} = fw_i \cdot \frac{1 t_{ACS^*}^{g-1}}{1 x_{CS^*}^{g-1}}$  if kid i of background g-1 is not a BK owner.  $lcaw_{i(g-1)} = fw_i \cdot \frac{t_{ACS^*}^{g-1}}{x_{S^{g-1}}^{g-1}}$  if kid i of background g-1 is a BK owner.

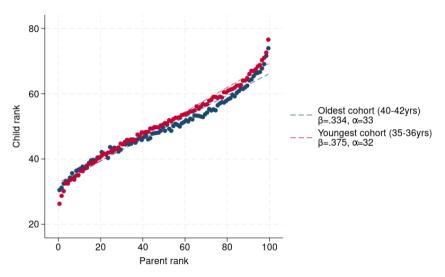
## Parent income by housing rank

Table: Parent average net income by housing asset rank

|      | None   | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | 10      | 11      |
|------|--------|--------|--------|--------|--------|--------|--------|--------|--------|---------|---------|
| mean | 40,470 | 32,270 | 37,070 | 40,910 | 43,830 | 46,660 | 50,140 | 53,570 | 70,760 | 87,110  | 272,800 |
| SD   | 64760  | 25,380 | 27,280 | 26,920 | 28,720 | 25,840 | 36,810 | 38,500 | 51,730 | 112,000 | 677,000 |

▶ Back

## Life-Cycle rank-rank relationships for income



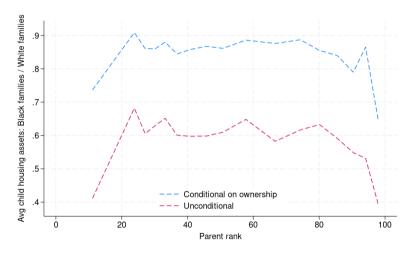
# Rank-Rank relationships in housing wealth over life cycle

Table:  $\alpha$  and  $\beta$  estimates across kid cohorts and weighting

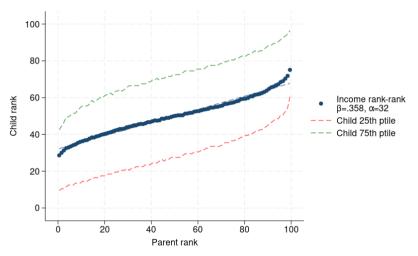
|          | All      | Ages     | Ages     | Ages     | LCA      |
|----------|----------|----------|----------|----------|----------|
|          | Cohorts  | 35-36    | 38-39    | 41-42    | weights  |
| $\beta$  | 0.305*** | 0.277*** | 0.303*** | 0.337*** | 0.424*** |
| $\alpha$ | 40       | 41       | 40       | 39       | 37       |



# Housing assets of children of Black families as a share of White assets

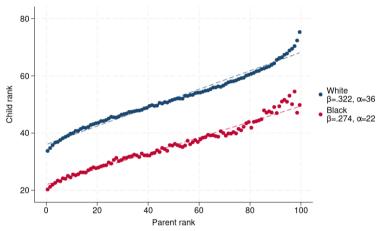


#### Rank-Rank estimates of income



• Compare Chetty et al. (2020) Income rank-rank  $\beta$ =0.35,  $\alpha$ =32.5

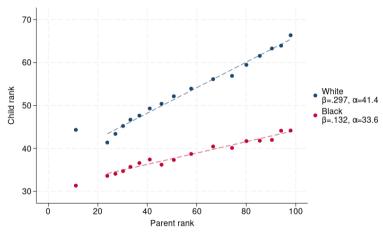
## Racial gaps in IGM of income



Compare Chetty et al. (2020) for Income:

• White  $\beta$ =0.32,  $\alpha$ =36.8; Black  $\beta$ =0.28,  $\alpha$ =25.4

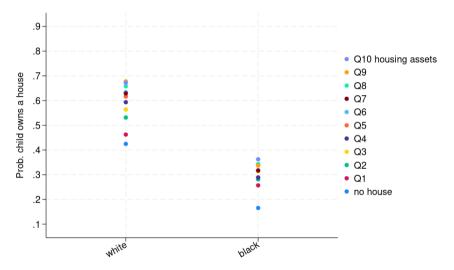
## Racial gaps in IGM of housing (no LCA weights)



Compare Chetty et al. (2020) for Income:

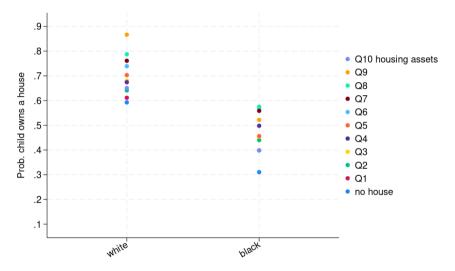
• White  $\beta$ =0.32,  $\alpha$ =36.8; Black  $\beta$ =0.28,  $\alpha$ =25.4

# Racial gaps in probability of home ownership (no LCA)





## Racial gaps in probability of home ownership, by income

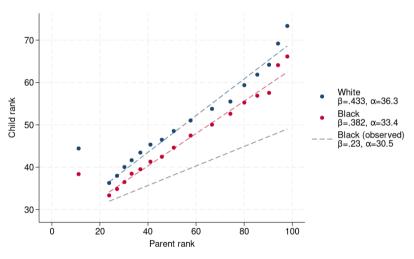


## Assigning counterfactual housing wealth ranks to Black renters

- Merge 2016-2021 ACS data on monthly rental payment to main dataset.
- Approach 1: Capitalize observed monthly rental payments *R* (for years 2018-2021).
  - What price P would make a risk-neutral investor indifferent about purchasing the unit.
  - Assume alternative rate of return a = .08 and housing rate of return h = .03.
  - User cost of capital implies  $P = \frac{12 \cdot R}{3 h} = 240 \cdot R$ .
  - Investor impatience would raise P while maintenance costs would lower P.
- Approach 2: Predict "starter" home values from observed renter-to-owner. Consider folks who were renting in 2016-2019 and also showed up as BK owners.
  - Regress log BK housing wealth on quadratic in log rent and parental background variables.
  - Predict BK housing wealth for observed Black renters in 2018-2021.
- Compute the (5<sup>th</sup>, 20<sup>th</sup>, 50<sup>th</sup>, 80<sup>th</sup>, 95<sup>th</sup>) pctile values, within each parental wealth vigintile, for each counterfactual.
- Randomly draw one of these numbers with probabilities (.10, .20, .40, .20, .10) in the simulation.
- Compute counterfactual ranks after assigning these counterfactual values.

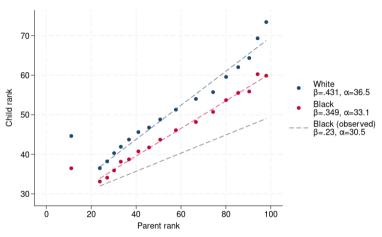


#### Counterfactual: Estimated from observed transitions



 $\bullet$  Reduces conditional gap  ${\approx}60\%$  in the bottom half and  ${\approx}72\%$  in the top half of the distribution

## Counterfactual: 25th pctile of observed owners



• Reduces conditional gap  ${\approx}45\%$  in the bottom quartile and  ${\approx}55\%$  in the top 3/4 of the distribution

## Joint relationship of parent housing and parent income

Table: Joint relationship of parent income and housing on child resources

|             | Child<br>Net Inc.      | Child<br>Housing       |
|-------------|------------------------|------------------------|
| Income      | 0.271***<br>(0.0013)   | 0.181***<br>(0.0011)   |
| Housing     | 0.175***<br>(0.0013)   | 0.290***<br>(0.0013)   |
| Interaction | -0.0003***<br>(0.0000) | -0.0004***<br>(0.0000) |
| constant    | 28.31***<br>(0.0564)   | 32.72***<br>(0.0705)   |

## Direct and indirect effects of parent resources on child housing

| Child:                        | Housing Wealth |                                | Housing Wealth     |
|-------------------------------|----------------|--------------------------------|--------------------|
| Parent:                       | Housing Wealth |                                | Housing Wealth     |
|                               |                |                                | Non-Housing Wealth |
| Eq. 1: Child Earnings $(Y_c)$ |                |                                |                    |
| Parent Housing                | 0.325***       | Parent Housing                 | 0.182***           |
|                               | (0.0008)       |                                | (0.0008)           |
|                               |                | Parent Non-housing             | 0.232***           |
|                               |                |                                | (0.0006)           |
| Eq. 2: Child Resources        |                |                                |                    |
| Child Labor                   | 0.549***       | Child Labor                    | 0.522***           |
|                               | (0.0009)       |                                | (0.0010)           |
| Parent Housing                | 0.266***       | Parent Housing                 | 0.241***           |
|                               | (0.0011)       |                                | (0.0013)           |
|                               |                | Parent Non-housing             | 0.039***           |
|                               |                |                                | (0.0011)           |
| Interaction $Y_c 	imes H_p$   | -0.0003***     | Interaction $Y_c \times H_p$   | -0.0005***         |
|                               | (0.0000)       |                                | (0.0000)           |
|                               |                | Interaction $Y_c \times Wnh_p$ | 0.0003***          |
|                               |                |                                | (0.0000)           |

# Estimating total wealth: Capitalization approach

Capitalize observed income flows to estimate wealth stocks, by source (j)

- $y_j = r_j * W_j \implies W_j = (1/r_j)y_j$
- use capitalization factors from PSZ for: fixed income assets (interest income), corporate assets (dividends and capital gains)
- use observed housing assets in our data
- capitalization factors for pension wealth using labor earnings and age profile from SZZ
- $\sum_{j} W_{j}$  and rank by total W

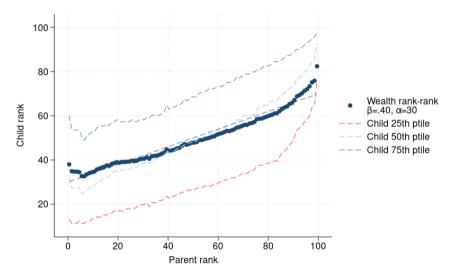
Key issues / assumptions:

- Don't need to get wealth right, just need to get ranks right at point in time
- Average over 3 years to reduce noise
- For the large majority of the distribution, Housing and Pensions are effectively the only assets. (i.e. robustness of capitalization factors only matters at the top)

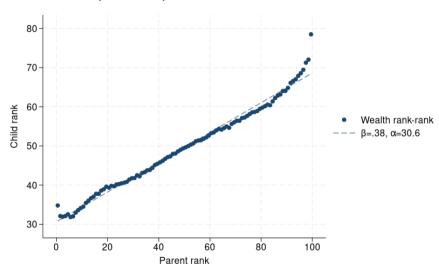
## Direct and indirect effects of parent resources on child resources

| Child:                        | Wealth     |                               | Wealth         | Capital Wealth |
|-------------------------------|------------|-------------------------------|----------------|----------------|
| Parent:                       | Wealth     |                               | Capital Wealth | Capital Wealth |
|                               |            |                               | Labor Wealth   | Labor Wealth   |
| Eq. 1: Child Earnings $(Y_c)$ |            |                               |                |                |
| Parent Wealth                 | 0.331***   | Parent Wealth                 | 0.220***       | 0.220***       |
|                               | (0.0006)   |                               | (0.0006)       | (0.0006)       |
|                               |            | Parent Labor                  | 0.176***       | 0.176***       |
|                               |            |                               | (0.0006)       | (0.0006)       |
| Eq. 2: Child Resources        |            |                               |                |                |
| Child Labor                   | 0.725***   | Child Labor                   | 0.725***       | 0.523***       |
|                               | (0.0007)   |                               | (8000.0)       | (0.0010)       |
| Parent Wealth                 | 0.203***   | Parent Wealth                 | 0.220***       | 0.217***       |
|                               | (0.0008)   |                               | (0.0000)       | (0.0010)       |
|                               |            | Parent Labor                  | -0.020***      | -0.028***      |
|                               |            |                               | (0.0009)       | (0.0011)       |
| Interaction $Y_c 	imes W_p$   | -0.0006*** | Interaction $Y_c \times CW_p$ | -0.0009***     | -0.0002***     |
|                               | (0.0000)   |                               | (0.0000)       | (0.0000)       |
|                               |            | Interaction $Y_c \times Y_p$  | 0.0004***      | 0.0006***      |
|                               |            |                               | (0.0000)       | (0.0000)       |

#### IGM of total wealth

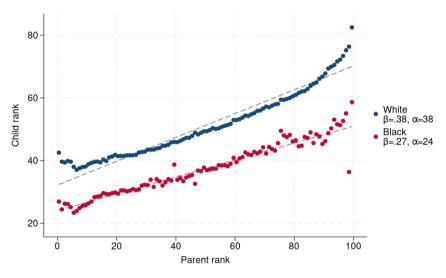


# IGM of total wealth (no LCA)



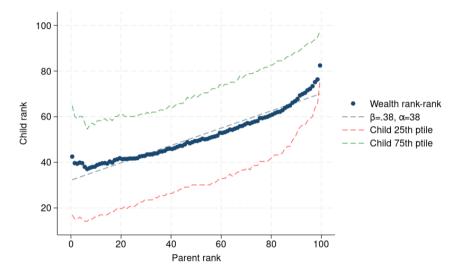


# IGM of total wealth by race





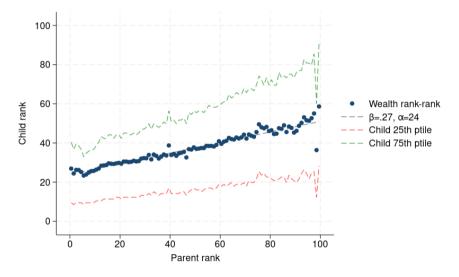
#### IGM of total wealth: White families





#### IGM of total wealth: Black families

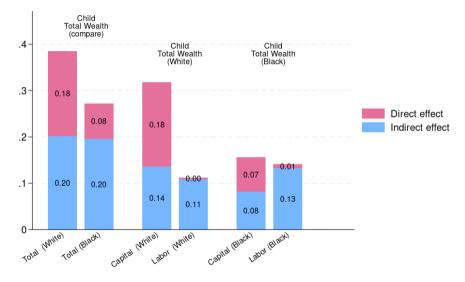
▶ Back



## Direct and indirect effects: Parent resources on child housing, by race

| Parent:                       | Housing Wealth |           | Housing Wealth                 |                    |           |
|-------------------------------|----------------|-----------|--------------------------------|--------------------|-----------|
|                               |                |           |                                | Non-Housing Wealth |           |
|                               | White          | Black     |                                | White              | Black     |
| Eq. 1: Child Earnings $(Y_c)$ |                |           |                                |                    |           |
| Parent Housing                | 0.294***       | 0.251***  | Parent Housing                 | 0.171***           | 0.129***  |
|                               | (0.0009)       | (0.0026)  |                                | (0.0010)           | (0.0028)  |
|                               |                |           | Parent Non-housing             | 0.206***           | 0.209***  |
|                               |                |           |                                | (0.0007)           | (0.0019)  |
| Eq. 2: Child Resources        |                |           |                                |                    |           |
| Child Labor                   | 0.529***       | 0.490***  | Child Labor                    | 0.510***           | 0.481***  |
|                               | (0.0011)       | (0.0023)  |                                | (0.0013)           | (0.0025)  |
| Parent Housing                | 0.286***       | 0.0722*** | Parent Housing                 | 0.265***           | 0.062***  |
|                               | (0.0013)       | (0.0034)  |                                | (0.0015)           | (0.0036)  |
|                               |                |           | Parent Non-housing             | 0.0322***          | 0.0194*** |
|                               |                |           |                                | (0.0013)           | (0.0030)  |
| Interaction $Y_c \times H_p$  | -0.0004***     | 0.0005*** | Interaction $Y_c \times H_p$   | -0.0005***         | 0.0003*** |
| ·                             | (0.0000)       | (0.0001)  | •                              | (0.0000)           | (0.0001)  |
|                               |                |           | Interaction $Y_c \times Wnh_p$ | 0.0003***          | 0.0003*** |
|                               |                |           | <u> </u>                       | (0.0000)           | (0.0001)  |

#### Direct and indirect effects: Parent resources on child wealth, by race



## Direct and indirect effects: Parent resources on child wealth, by race

| Parent:                       | Total Wealth |            | Parent: Total Wealth          |            |            | Capital<br>Labor ' | Wealth<br>Wealth |
|-------------------------------|--------------|------------|-------------------------------|------------|------------|--------------------|------------------|
|                               | White        | Black      |                               | White      | Black      |                    |                  |
| Eq. 1: Child Earnings $(Y_c)$ |              |            |                               |            |            |                    |                  |
| Parent Wealth                 | 0.301***     | 0.247***   | Parent Cap Wealth             | 0.202***   | 0.112***   |                    |                  |
|                               | (0.0006)     | (0.0016)   |                               | (0.0007)   | (0.0019)   |                    |                  |
|                               |              |            | Parent Labor                  | 0.162***   | 0.182***   |                    |                  |
|                               |              |            |                               | (0.0007)   | (0.0018)   |                    |                  |
| Eq. 2: Child Resources        |              |            |                               |            |            |                    |                  |
| Child Labor                   | 0.707***     | 0.736***   | Child Labor                   | 0.702***   | 0.741***   |                    |                  |
|                               | (0.0010)     | (0.0018)   |                               | (0.0011)   | (0.0021)   |                    |                  |
| Parent Wealth                 | 0.218***     | 0.0839***  | Parent Cap Wealth             | 0.243***   | 0.0764***  |                    |                  |
|                               | (0.0009)     | (0.0021)   |                               | (0.0011)   | (0.0025)   |                    |                  |
|                               |              |            | Parent Labor                  | -0.0337*** | 0.0117***  |                    |                  |
|                               |              |            |                               | (0.0010)   | (0.0024)   |                    |                  |
| Interaction $Y_c \times W_p$  | -0.0006***   | -0.0002*** | Interaction $Y_c \times CW_p$ | -0.0010*** | -0.0000    |                    |                  |
| ,                             | (0.0000)     | (0.0000)   | •                             | (0.0000)   | (0.0000)   |                    |                  |
|                               |              | -          | Interaction $Y_c \times Y_p$  | 0.0006***  | -0.0002*** |                    |                  |
|                               |              |            | ,<br>                         | (0.0000)   | (0.0001)   |                    |                  |

## Decomposing racial IGM gaps in wealth



## Decomposition of indirect effect into income levels and income returns

- Given a set of initial  $(\rho_y, \gamma_y)$  values, the change in the indirect effect from a given exposure is  $(\rho_y + \theta_\rho)(\gamma_y + \theta_\gamma) \rho_y \gamma_y$ .
- Splitting the cross term yields "income levels" channel of  $\theta_{\rho}(\gamma_y + \theta_{\gamma}/2)$  and "income returns" channel of  $\theta_{\gamma}(\rho_y + \theta_{\rho}/2)$ .
- Recall that we have already estimated the total change in the indirect effect  $\theta_{\iota}$ .
- Assumption: the initial values implicit in the comparison are given by the population means modified by the exposure coefficients times a common unknown scalar  $\sigma$ . (i.e. "proportional scaling")
- This yields the following equation:  $\theta_{\iota} = \theta_{\rho}(\overline{\gamma_{y}} \theta_{\gamma}\sigma + \theta_{\gamma}/2) + \theta_{\gamma}(\overline{\rho_{y}} \theta_{\rho}\sigma + \theta_{\rho}/2)$
- Solving yields  $\sigma = \frac{\theta_{\rho} \overline{\gamma_{y}} + \theta_{\gamma} \overline{\rho_{y}} + \theta_{\gamma} \theta_{\rho} \theta_{\iota}}{2\theta_{\gamma} \theta_{\rho}}$
- Substituting this value back into the above expression and canceling terms yields decomposition equation (5).

#### Results for White families

Table: Associations between County-Level Exposures and Housing Wealth Mobility

| Exposure  | $\alpha$         | eta and its decomposition |                    |                   |                   |
|---|------------------|---------------------------|--------------------|-------------------|-------------------|
|   |                  | Total                     | Direct effect      | Income returns    | Income levels     |
| GR unemployment shock (p.p. increase / 100)         | 731***<br>(.042) | 1.062***<br>(.099)        | 0.365***<br>(.076) | .214***<br>(.026) | .483***<br>(.030) |
| Exposure mean, SD, N: .046                          | 6, .022, 3100    |                           |                    |                   |                   |
| Housing supply elasticity (dlog units / dlog price) | 045***<br>(.011) | 380***<br>(.029)          | 226**<br>(.023)    | 067***<br>(.010)  | 087***<br>(.019)  |
| Exposure mean, SD, N: .310, .120, 800               |                  |                           |                    |                   |                   |

Mobility data source: IRS federal income tax returns linked to 2000 Census Long Form and Black Knight property records.

Great Recession shock data source: BLS Local Area Unemployment Statistics

Housing supply data source: Baum-Snow and Han (2024)

#### Results for Black families

Table: Associations between County-Level Exposures and Housing Wealth Mobility

| Exposure  | α                | eta and its decomposition |                 |                   |                  |
|---|------------------|---------------------------|-----------------|-------------------|------------------|
|   |                  | Total                     | Direct effect   | Income returns    | Income levels    |
| GR unemployment shock (p.p. increase / 100)         | 0.117*<br>(.066) | 502<br>(.360)             | 396<br>(.296)   | 0.201**<br>(.098) | 307***<br>(.096) |
| Exposure mean, SD, N: .049                          | , .021, 1000     | 0                         |                 |                   |                  |
| Housing supply elasticity (dlog units / dlog price) | 002<br>(.018)    | 037<br>(.061)             | 0.005<br>(.047) | 029<br>(.040)     | 013<br>(.040)    |
| Exposure mean, SD, N: .294                          | , .129, 500      |                           |                 |                   |                  |

Mobility data source: IRS federal income tax returns linked to 2000 Census Long Form and Black Knight property records.

Great Recession shock data source: BLS Local Area Unemployment Statistics

Housing supply data source: Baum-Snow and Han (2024)

